

COMSEFOR: Computer Security and Formal methods

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Abstract

We propose to design, develop and experiment a new approach of formal security proofs.

One of the main issues in formal security proofs is to design an attacker model. Such a model is always disputable; even when a proof is completed in some model, one can find an attack in another model.

This project aims at bypassing the problem, roughly by specifying what an attacker *cannot* do, instead of specifying what he/she can do.

1 The context

1.1 Software security

The development of distributed applications that send and receive informations from other sources is both an opportunity and a threat. Let me give some examples.

Internet banking and, more generally Internet transactions, increases our comfort, avoiding a move (and possibly a queue) at the bank/merchant's location. Furthermore, the services are available at any time and from any place. It is therefore an opportunity, but it is also a threat since confidential information, such as credit card numbers or any other credentials, is sent over an insecure communication channel.

Mobile phones offer geo-localisation, which is very convenient for finding our way. It is also a threat since this information could be eavesdropped, while we wish to keep it private. This observation applies to many on-line services that are very convenient, but leak information about ourselves. Big Brother is not far.

In the medical area, it will be very convenient to wear devices that send measures such as our blood pressure, our temperature... and receive instructions from the medical center on how the device should react. However, we can imagine that an attacker could send wrong information. In 2013, the US vice-president Dick Cheney feared a terrorist attack on his pacemaker.

This observation also applies to many other embedded devices. In 2015, we were not surprised to learn that it is possible to mount remote attacks on a vehicle, taking the control of the car (<http://argus-sec.com/car-hacking/>).

Not only terrorists are a threat. As the PRISM scandal shows, also those whose intentions are noble may get some information that we want to keep confidential.

There are numerous other examples. There will be more and more in the future. We wish to take advantage of these new technologies. We also wish to limit the threats as much as possible. To achieve this goal and get the best without the risks, the programs aim at achieving security goals. They use security primitives such as encryption, digital signatures, zero-knowledge proofs ... Can we trust them ?

1.2 Safety vs security. The role of formal methods

The issue of “hunting the bugs” is not new. Several methods and tools have been designed in the past 50 years. Typically, embedded software (on cars, aircrafts, spaceships) attracted some attention. This yield verification algorithms, proof systems, testing methods... that have proved their usefulness and have significantly increased the safety of critical applications: the programs are more often implementing their expected functionality.

Security is different from safety. In the case of security properties, we must show that some property is satisfied, in the presence of an arbitrary adversary. At first sight this looks similar to the verification of a controller, whose goal is to bring back the system to a safe state, whatever the actions of the environment are. There is however a major difference. For classical safety properties, the actions of the controller depend on its observations. In the case of security, the (honest) programs may not even notice that an attack is going on: often there are no observations available.

Therefore the classical model-checking techniques that have been developed during the last decades cannot be (at least not directly) used for security.

Similarly, other techniques such as statistical testing are not relevant,

because whatever distribution of events is used for testing, the attacker need not comply with such a distribution. More generally, we can expect an attacker to rely on any security breach whatsoever. That is why formal methods play an important role in increasing our confidence in the security of programs.

In the remainder of the project, we will focus on security protocols (the distributed programs, as in the above examples). The same ideas might be used for other programs/circuits aiming at some security goal. This is not discussed in this project, but might be the subject of future work.

1.3 What is an attacker ?

We have explained why formal methods play an important role in computer security. However, a formal analysis of a security application/protocol requires a formal definition of the attacker. This is a central question and a starting point of our project. We first investigate the various attacker models that have been considered so far.

The Dolev-Yao attacker In their seminal work D. Dolev and A. Yao [21] define a formal model, in which the attacker is a device that sits in the middle of every communication. The attacker eavesdrops on all messages, builds new messages according to a fixed set of rules and sends messages (impersonating the sender). The scope of their framework is very limited (only public-key encryption, a fixed set of pairs sender/receiver, a “ping-pong” control structure,...) but since then, many extensions have been designed along the same lines. The protocols are now specified in a process algebra that embeds security primitives, such as the applied pi calculus [2]. Several automatic verification tools have been designed, relying on what is now known as “the Dolev-Yao attacker”. Among the most recent ones, let me cite PROVERIF [18] or SCYTHET [20], but there are many more.

Following Dolev and Yao, all these works see messages as terms constructed on black-box cryptographic primitives, whose properties are specified equationally. The attacker can only use such primitives to build or analyse the messages.

While this approach has been proved to be successful in finding attacks (see for instance [1]), proofs of protocols in these models should be taken with care. Indeed, the attacker model is a bit rough; nothing prevents an attacker from using any other computation mechanism than the fixed set of primitives that are given to him/her in this model. For instance there are protocols that have been proved secure in the Dolev-Yao model and for

which attacks were found later. This is the case for instance of the Needham-Schroeder-Lowe (NSL) protocol [33] and Bull's authentication protocol [30].

The latter example, as well as others, were a motivation for introducing equational properties of the security primitives, or additional capabilities of the attacker. Several tools such as ProVerif [18] or TAMARIN [26] implement some restricted properties of the primitives.

The other example (the attack on the NSL protocol) is more difficult. It relies mainly on the malleability of an encryption scheme: the attack can be mounted if it is possible to build a ciphertext from another ciphertext, without holding the decryption key. This is possible for instance with the El Gamal encryption scheme [22]. If we wish to capture such an attack, we need to give the attacker such a capability. What should exactly be the extra capabilities of the attacker is however not clear. It depends on the actual encryption scheme and on the implementation of other primitives.

The computational attacker A more accurate attacker model has been adopted by the cryptographers, following Golwasser and Micali [23]. As in the Dolev-Yao case, the attacker may eavesdrop on messages and build fake messages. However, he/she is not any more limited by a fixed set of possible operations. He/she may now perform any computation that can be completed in probabilistic polynomial time (in the worst case). The input of such an attacker is a security parameter (roughly, the length of the encryption keys).

Now, there is always a chance that an attacker will succeed, since he/she may simply guess the key correctly. In this context, a protocol is secure if the success probability of an attacker is bounded by a function of the security parameter, which decreases quickly when the security parameter grows; security is an asymptotic property.

This model of attacker is currently the most accurate one for which formal proofs and formal tools are available. For instance CRYPTOVERIF [13] is a prover that automatically reduces cryptographic games to simpler games. In the initial game, the attacker plays against the protocol and in the final game an attacker plays against a presumably hard problem (such as discrete logarithm, or IND-CPA if the encryption scheme is assumed to satisfy such a property). The probability of success of an attacker on a given game is computed as a function of the probability of success of the attacker in the previous game. Then, the protocol is secure if the probability of success of the attacker in the initial game is not significantly larger than the probability of success of the attacker on the presumably hard problem.

CRYPTOVERIF has had a number of successes in proving protocols in this setting. Though the library of games and strategies is continuously increasing, there are still many situations that require the user to add a new game or to interact with the tool in order to guide the reduction strategy. In some cases, CRYPTOVERIF simply fails to prove the protocol.

EASYPYPT [9] shares several features with CRYPTOVERIF: it also works by successive reductions, however at a lower level, as it deals with individual commands. This allows for more flexibility and, in principle, a broader scope of applications. It is however a proof assistant, which requires interactions with the user. So far, it was mostly successful in proving/attacking complex cryptographic primitives (see for instance [10]), not yet full protocols.

In both cases, there is no full automation: the default strategy is likely to fail on many inputs. Another issue is the composability of proofs, which is necessary for relatively large protocols. Most importantly, proof attempts may fail. Does it mean that we have not put sufficient effort in completing the proof? Or does it mean that there is an attack?

On the other hand, these tools provide the user with quantitative information on the probability of success of an attacker (which we do not expect to obtain in our project).

Computational soundness Another line of research, which was initiated by M. Abadi and P. Rogaway [3], consists in trying to get the best of the previous two models (the Dolev-Yao one and the computational one). The idea is to prove a “full abstraction” result for a Dolev-Yao style attacker. Such results are now known as “computational soundness results”. They list the computational assumptions, under which a Dolev-Yao attacker is equally (up to negligible probability) likely to mount an attack than the computational attacker.

Abadi and Rogaway [3] consider a passive attacker, symmetric encryption and equivalence properties. Further papers, for instance [6, 4, 19, 15] but there are many more, extend this idea to active attacks, other primitives and/or other security properties.

Those works provide nice hints on which properties of the primitives are relevant. As shown in [16], they require a lot of assumptions, some of which are not realistic: no key cycle is ever created (this is undecidable), the keys are honestly generated (meaning that they always come with a certificate), there is a polynomial parsing algorithm from bitstrings to terms (this does not exist for some primitives),.... Furthermore, the computational soundness

proofs tend to be extremely complicated, hence difficult to check.

Modularity As the attacker model becomes more accurate, the proofs become more complex. When a protocol combines several subprotocols or uses several primitives, it is necessary to decompose the proofs. This was the main motivation for the introduction of the “universal composability” property [14]. This property is however difficult to prove (and actually to define precisely, as there were several successive definitions). It has also some limitations (see for instance [25]), related to the “commitment problem”: there is no UC proof for primitives that first commit on some hidden value and then reveal that value.

Up to now, there is no formal tool that would complete or check universal composability proofs.

More powerful attackers One could also wonder whether the computational attacker, as defined above, is the best possible definition. There were several criticisms, mainly on the asymptotic nature of the security guarantees in this model [24]. But there are other questions. For instance, why is it a machine running in worst-case probabilistic polynomial time ? why not (for instance) in average probabilistic polynomial time ? Or subexponential probabilistic polynomial time ? As far as I understand, the reason is to consider a class of machines, which is closed by composition; the motivations are not the accuracy of the model.

Anyway, we may realistically imagine more powerful attackers. For instance attackers that have some other channels through which they may get side information. It could be the observation of time or power consumption in the execution of a program, for instance. The attacker could also corrupt some package updates, which replace cryptographic primitives by fake implementations, yet undetectable by the user (see for instance [12]).

Conclusion It seems that we are faced with a dilemma: the more accurate the attacker model is, the more difficult the security proofs are. Already for the computational attacker, it is very difficult to complete security proofs automatically.

Is such an increasing complexity of the proofs unavoidable when the attackers becomes more powerful ? We will show that the answer is no. There is a way out.

2 Our approach

2.1 A universal attacker ?

We propose in [7, 8] a new approach, which overcomes some of the above mentioned shortcomings. This approach is also described in G. Scerri's thesis [31].

The main idea is to consider an attacker that can a priori perform any computation, unless it breaks some assumptions. In other words, instead of specifying the attacker's capabilities, as the Dolev-Yao and computational model do, we specify what an attacker cannot do; we consider the most powerful attacker that does not break some (first-order) axioms.

Given such axioms A , a security property ϕ and the conditions θ that gather the tests performed along a protocol execution, the security of the protocol reduces to the inconsistency of $A \cup \{\neg\phi, \theta\}$. Conversely, the consistency of such a set of formulas implies the existence of a model, which witnesses an attack.

Example

Let us give a very simple example. The precise definitions are missing and the example might be difficult to follow in details. The goal is to give a flavor of the method.

We consider a logic that includes a variadic predicate \triangleright . The intended meaning of $T \triangleright t$ is that an attacker may compute t from T . This can be interpreted in the computational setting, using a Kripke semantics, in which the worlds are the non-negligible sets of samplings; $T \triangleright t$ is valid in the computational semantics, if, for any non-negligible S , there is a non-negligible $S' \subseteq S$ and a probabilistic polynomial time Turing machine \mathcal{A} , such that for the samplings $\tau \in S'$, given the interpretation of T w.r.t. τ , \mathcal{A} computes the interpretation of t w.r.t. τ .

We consider two axiom schemes:

$$\mathit{fresh}(X, n) : \quad X \not\ni n$$

which states (roughly) that, if a name n does not occur in a set X , then the attacker cannot compute n . In the computational semantics, this statement is valid, since, without any information on n , the attacker can only guess n with a negligible probability.

$$\mathit{usable}(X \cup x, k), \mathit{fresh}(X \cup x, r) : \quad X, \mathit{enc}(x, k, r) \triangleright n \quad \rightarrow \quad X \triangleright n$$

which states that an encryption with a usable key k does not bring any significant additional information for computing n ; if n can be computed with

the ciphertext, then it can be computed without it. The definition of *usable* depends on the assumptions on the encryption scheme. The simplest case is to assume that the encryption key k does not appear as a plaintext in X, x (only as an encryption key). In the computational model, such an axiom is valid for IND-CPA encryption schemes that are which-key concealing, as shown in [31].

Now, if a protocol consists in sending out a single message $\text{enc}(n, k, r)$ and we wish to prove that the random number n is secret, it is sufficient to prove that the axioms, together with $\text{enc}(n, k, r) \triangleright n$ (the negation of the security property) are inconsistent. This is the case since, for an empty set X , the second axiom yields $\emptyset \triangleright n$, which contradicts the first axiom.

As a consequence, this trivial protocol is secure, for any attacker and cryptographic primitives that satisfy the two axioms. This is in particular the case for a computational attacker, when the encryption scheme is IND-CPA and which key concealing.

This approach is very appealing, as we could, for instance, complete proofs in the computational model, while staying within first-order logic. We do not need any of the hypotheses of computational soundness proofs and still avoid the machine reductions and probabilities computations. There are still a number of questions:

Axioms What are the axioms ? How to design them ? How can we show their relevance ?

Proof search A priori, the consistency of first-order formulas is undecidable. Do we really gain something ?

Case studies Is the method of any practical use ? Can we discover new attacks ?

Modularity Can we decompose the proofs of complex protocols into smaller pieces ? Can we re-use some proofs ?

Security properties Which security properties can be specified ?

Some of these questions have been (at least partly) answered in the thesis of Guillaume Scerri (defended on January 2015), some others are part of this project.

2.2 G. Scerri's thesis

Axioms In G. Scerri's thesis, a number of axioms are proposed, which reflect some classical properties of encryption schemes, such as IND-CPA [23], or integrity [11]. They are proved to be valid in a computational model. Therefore, the inconsistency of the set of formulas implies computational security.

Proof search In general, the consistency of a set of first-order formulas is undecidable. However, in the case of the above axioms (and a confidentiality property) the consistency problem is decidable. It is even in PTIME [17] if we do not include the most general integrity axiom.

Case studies A prototype verification tool (SCARY) has been implemented (by G. Scerri), which is encouraging. For instance known and also new attacks have been found [31].

2.3 A summary of our research program

The preliminary results that are reported above encourage us to develop the approach further and experiment it at a larger scale.

This includes the investigation of another logic that embeds indistinguishability properties (section 3), the design of modular proofs (section 4), the design of additional axioms, for instance axioms about new cryptographic primitives (section 5), experimentations on a larger scale (section 6) and considering side channels attacks (section ??).

3 Task 1: Indistinguishability properties

We have recently designed [8] another logic that embeds indistinguishability properties. This logic is simpler than the previous one, but it is not yet clear how easy (or difficult) it will be to automate.

We first need to study more examples, which will witness the relevance of the set of axioms that we have, or, to the contrary, require new axioms that we will have to design.

Then, the main task will be to design appropriate strategies and possibly to prove tractability results in the spirit of [17]. Depending on the outcome, we will (or not) implement another tool, based on this logic. If the logic turns out to be easily decidable, we need to carry experiments on practical case studies. If the logic turns out to be undecidable or too complex, we will focus more on the development of the SCARY tool.

4 Task 2: Proof (de)composition

Our method has some inherent composability properties: when a protocol P_1 is proved secure, adding more axioms will restrict the attacker’s capabilities, not increase them. Therefore, the protocol P_1 will remain secure.

If we add a new protocol P_2 that runs in parallel of the protocol P_1 , we need however to revise the former security proof. P_2 introduces more traces, some of which may violate the security property. In general, proving P_1 and P_2 separately does not imply that, together, they are secure.

Still, our framework provides with a possible solution for composing the proofs. First observe that, if the axioms A_1 that are used in the security proof of P_1 , are sound in the presence of a computational attacker that has an access to P_2 (as an oracle), then the security of P_1 holds for this stronger model of attacker. This implies in particular that, if in addition P_2 alone is secure, then P_1 and P_2 together are secure.

Now, proving that an axiom A_1 is sound with respect to an attacker that has access to P_2 as an oracle, could again benefit from our approach. We could see A_1 as a security property that has to be satisfied by P_2 , this time considering a (simple) computational attacker.

In summary, we would have to prove that $\neg A_1 \cup A_2 \cup \theta_2$ is inconsistent for any constraint θ_2 generated by a trace of P_2 and then the inconsistency of $\neg\phi \cup A_1 \cup A_2 \cup \theta_1$ for any constraint generated by a trace of P_1 , where ϕ is the security property.

Though this looks easy in theory, there are some hidden difficulties. For instance, currently, the logical fragment in which the axioms are defined is different (and larger) than the fragment in which the security properties are defined. This feature is used in the design of efficient strategies. Also, once more, we need concrete examples and experiments to test the practical relevance of such an idea.

5 Task 3: Axiom design

Though a number of axioms are designed and proved to be sound in the computational model in [31], they only concern the classical properties of encryption. As for indistinguishability properties, very few axioms were considered in [8]. We need to design and prove axioms for other primitives, under various assumptions and in different logics.

One of the challenges, which would be interesting to investigate, is the case of exclusive-or. Indeed, [5, 32] (for instance) show that it is impossible

to design a computational soundness result for exclusive-or. This means that we cannot specify equationally (and independently of the security parameter) what an attacker can do. But what about what an attacker cannot do ?

Another challenge concern the hash functions, for which similar impossibility results have been proved.

There are easier cases that should be investigated first, such as signatures, zero-knowledge proofs and possibly others.

6 Task 4: Automation and case studies

Although the consistency checks can often be completed in polynomial time, we need to complete such a check for every possible sequence of control states. In principle, we have to consider any interleaving of control states of the processes. Therefore, there are in principle exponentially many sequences of control states that have to be considered.

If we want to consider significant case studies, it is necessary to improve upon such a naive implementation. There are several directions that can be investigated. First, the deductions that are performed on some branch should be re-used (when relevant) in other branches. Sharing more deductions across branches may require us to modify the saturation strategy. In summary: we have to design an efficient saturation strategy for each trace, which also takes into account the possible further reuse of intermediate deductions. There is some hope here since, for instance, the same axioms and security property are used on each trace.

Another direction that could yield dramatic improvements are partial order reductions, such as in [28].

In the case of equivalence properties (see section 3), the problem is different, as all traces are folded in a single one [8]. However, the very folding process, as well as the proof strategies, deserves attention.

In the end, the goal is to find unexpected attacks on well-known protocols, which were proved using various tools, but with a weaker attacker model ! We especially target widely deployed protocols such as Kerberos [29]. But we also expect to automatically analyse protocols that are currently beyond the scope of the existant automatic provers, because they use both complex primitives and equivalence properties.

7 Task 5: Beyond the computational attacker

In the section 4, we have seen a possible use of an attacker, who is stronger than the computational one (because it may have access to external oracles).

An advantage of our approach is that it works for any model of attacker. So far, we have only considered applications to the computational attacker, reducing the computational security to the inconsistency of a set of first-order formulas. Such an inconsistency result however implies something stronger: the security w.r.t. any model of attacker that satisfies the axioms. If we design the axioms in such a way that they are valid for other models of attackers, we will get security guarantees for such attackers.

As an example, we could consider an attacker who also observes execution time. Such an attacker will distinguish messages that require different computation times. We could design axioms that state the indistinguishability (w.r.t. computation time) of some basic operations and guard the other indistinguishability axioms by such indistinguishability computation times. In such a setting, an inconsistency proof would show the security in presence of an attacker who may observe the execution time. Conversely, a model would be a witness of an attack that exploits such observations.

Similar methods can be applied to the power consumption observation, for instance [27].

In this last task we will investigate security proofs for several such stronger attackers.

References

- [1] Spore, the security protocol open repository. [//www.lsv.ens-cachan.fr/spore](http://www.lsv.ens-cachan.fr/spore).
- [2] M. Abadi and C. Fournet. Mobile values, new names, and secure communication. In *Proceedings of the 28th ACM Symposium on Principles of Programming Languages (POPL'01)*, pages 104–115, January 2001.
- [3] M. Abadi and P. Rogaway. Reconciling two views of cryptography (the computational soundness of formal encryption). *J. Cryptology*, 15(2):103–127, 2002.
- [4] M. Backes and B. Pfitzmann. Symmetric encryption in a simulatable dolev-yao style cryptographic library. In *Proc. IEEE Computer Security Foundations workshop*, 2004.

- [5] M. Backes and B. Pfitzmann. Limits of the cryptographic realization of Dolev-Yao style XOR. In *Proc. 10th European Symposium on Research in Computer Security (ESORICS)*, 2005.
- [6] M. Backes, B. Pfitzmann, and M. Waidner. A composable cryptographic library with nested operations. In *Proc. 10th ACM Conference on Computer and Communications Security (CCS'03)*, 2003.
- [7] G. Bana and H. Comon-Lundh. Towards unconditional soundness: Computationally complete symbolic attacker. In P. Degano and J. D. Guttman, editors, *Proceedings of the 1st International Conference on Principles of Security and Trust (POST'12)*, volume 7215 of *Lecture Notes in Computer Science*, pages 189–208. Springer, Mar. 2012.
- [8] G. Bana and H. Comon-Lundh. A computationally complete symbolic attacker for equivalence properties. In *Proc. ACM Conference on Computers and Communications Security*, 2014.
- [9] G. Barthe, F. Dupressoir, B. Grgoire, C. Kunz, B. Schmidt, and P. Strub. Easycrypt: a tutorial. In *Foundations of security analysis and design vii*. Springer international publishing, 2014.
- [10] G. Barthe, B. Grégoire, Y. Lakhnech, and S. Z. Béguelin. Beyond provable security verifiable IND-CCA security of OAEP. In A. Kiayias, editor, *Topics in Cryptology - CT-RSA 2011 - The Cryptographers' Track at the RSA Conference 2011, San Francisco, CA, USA, February 14-18, 2011. Proceedings*. Springer, 2011.
- [11] M. Bellare and C. Namprempe. Authenticated encryption: relations among notions and analysis of the generic composition paradigm. In *Advances in Cryptology – ASIACRYPT 2000*, volume 1976 of *Lecture Notes in Computer Science*, pages 531–545, Kyoto, 2000.
- [12] M. Bellare, K. G. Paterson, and P. Rogaway. Security of symmetric encryption against mass surveillance. In *Proc. CRYPTO*, 2014.
- [13] B. Blanchet. A computationally sound mechanized prover for security protocols. In *2006 IEEE Symposium on Security and Privacy (S&P 2006), 21-24 May 2006, Berkeley, California, USA*, pages 140–154. IEEE Computer Society, 2006.
- [14] R. Canetti. Universal composable security: a new paradigm for cryptographic protocols. In *Proc. 42nd IEEE Symposium on Foundations of Computer Science*, 2001.

- [15] H. Comon-Lundh and V. Cortier. Computational soundness of observational equivalence. In *Proceedings of the 15th ACM Conference on Computer and Communications Security (CCS'08)*, pages 109–118. ACM Press, Oct. 2008.
- [16] H. Comon-Lundh and V. Cortier. How to prove security of communication protocols? a discussion on the soundness of formal models w.r.t. computational ones. In *Proceedings of the 28th Annual Symposium on Theoretical Aspects of Computer Science (STACS'11)*, volume 9 of *Leibniz International Proceedings in Informatics*, pages 29–44, Dortmund, Germany, 2011. Leibniz-Zentrum für Informatik.
- [17] H. Comon-Lundh, V. Cortier, and G. Scerri. Tractable inference systems: an extension with a deducibility predicate. In *Proceedings of the 24th International Conference on Automated Deduction (CADE'13)*, volume 7898 of *Lecture Notes in Artificial Intelligence*, Lake Placid, New York, USA, 2013. Springer.
- [18] V. Cortier and S. Kremer, editors. *Formal Models and Techniques for Analyzing Security Protocols*, chapter Using Horn Clauses for Analyzing Security Protocols, pages 86–111. IOS Press, 2011.
- [19] V. Cortier and B. Warinschi. Computationally sound, automated proofs for security protocols. In *Proceedings of the 14th European Symposium on Programming (ESOP'05)*, volume 3444 of *Lecture Notes in Computer Science*, pages 157–171, Edinburgh, U.K, April 2005. Springer.
- [20] C. Cremers. The Scyther Tool: Verification, falsification, and analysis of security protocols. In *Computer Aided Verification, 20th International Conference, CAV 2008, Princeton, USA, Proc.*, volume 5123/2008 of *Lecture Notes in Computer Science*, pages 414–418. Springer, 2008.
- [21] D. Dolev and A. Yao. On the security of public key protocols. In *Proc. IEEE Symp. on Foundations of Computer Science*, pages 350–357, 1981.
- [22] T. E. Gamal. A public key cryptosystem and a signature scheme based on discrete logarithms. *IEEE Transactions on Information Theory*, 31, 1985.
- [23] S. Goldwasser and S. Micali. Probabilistic encryption. *Journal of Computer and Systems sciences*, 28, 1984.

- [24] N. Koblitz and A. Menezes. Another look at provable security. *Journal of Cryptology*, 20(1), 2007.
- [25] Y. Lindell. General composition and universal composition in secure multiparty computation. In *Proc. 44th IEEE Symp. Foundations of Computer Science (FOCS)*, 2003.
- [26] S. Meier, B. Schmidt, C. Cremers, and D. A. Basin. The TAMARIN prover for the symbolic analysis of security protocols. In *Computer Aided Verification - 25th International Conference, CAV 2013, Saint Petersburg, Russia, July 13-19, 2013. Proceedings*, pages 696–701, 2013.
- [27] S. Micali and L. Reyzin. Physically observable cryptography (extended abstract). In *Proc. Theory of Cryptography, First Theory of Cryptography Conference, TCC 2004, Cambridge, MA, USA, February 19-21, 2004, Proceedings*, pages 278–296, 2004.
- [28] S. Mödersheim, L. Vigano, and D. Basin. Constraint differentiation: Search-space reduction for the constraint-based analysis of security protocols. *Journal of Computer Security*, 2010.
- [29] B. C. Neuman and T. Ts'o. Kerberos: An authentication service for computer networks. *IEEE Communications*, 32, 1994.
- [30] P. Ryan and S. Schneider. An attack on a recursive authentication protocol: A cautionary tale. *Information Processing Letters*, 65, 1998.
- [31] G. Scerri. *Proofs of security protocols revisited*. PhD thesis, École Normale Supérieure de Cachan, 2015.
- [32] D. Unruh. The impossibility of computationally sound xor, July 2010. Preprint on IACR ePrint 2010/389.
- [33] B. Warinschi. A computational analysis of the needham-schroeder protocol. In *16th Computer security foundation workshop (CSFW)*, pages 248–262. IEEE, 2003.